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### Durable Goods, Investment Shocks and the Comovement Problem\*

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#### Abstract

Recent research based on sticky-price models suggests that capital investment shocks are an important driver of business cycle fluctuations. Despite their quantitative importance in explaining business cycles, a comovement problem emerges because the shocks generate an intertemporal substitution effect away from consumption toward investment. This paper resolves the comovement problem by extending the standard neoclassical sticky-price model to a two-sector model with consumer durable services. When durable goods are used as investment in capital and consumer durables, positive capital investment shocks also generate an intratemporal substitution effect away from consumption that dominates the intertemporal effect. As a result, consumption increases, and the comovement problem is resolved.

Keywords: Investment shocks; Durables; Sticky prices; Comovement

JEL classification: E21; E22; E32

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#### 1. Introduction

Recent research suggests that an important driver of business cycle fluctuations are not more traditional Hicks-neutral technology shocks (Galí, 1999), but (equipment) capital investment-specific technology shocks (e.g., Greenwood et al., 2000; Christensen and Dib, 2008; Justiniano and Primiceri, 2008). Recently, using a one-sector model, Fisher (2006) estimated and found that capital investment shocks were the dominant source of business cycle fluctuations in the U.S. In particular, Justiniano et al. (2010) studied a one-sector, sticky-price model with a variety of real and nominal frictions such as wage rigidities, consumption habit formation and capital utilization, along the lines of Christiano et al. (2005), and several shocks, as in Smets and Wouters (2007), including a shock to total factor productivity (or a neutral technology shock), as in Kydland and Prescott (1982) and Hansen (1985); a shock to the marginal efficiency of investment (or, for simplicity, an investment shock), as in Greenwood et al. (1988) and Greenwood et al. (1997); and a shock to desired wage markups (or, equivalently, a labor supply shock), as in Hall (1997). They found that over 50% of the fluctuations in output and hours, and over 80% of the fluctuations in investment were driven by capital investment shocks.

Even though capital investment shocks are of quantitative importance in explaining business cycle fluctuations, one difficulty remains in these models: consumption typically falls after a positive investment shock, which is at odds with the data that consumption and investment both increase in response to a positive capital investment shock.<sup>1</sup> A comovement problem emerges because a positive investment shock generates an intertemporal substitution effect away from current consumption and toward current investment and thus future consumption which dominates the income effect. As a result, these models do not result in comovements among macroeconomic aggregates in response to an investment shock, unlike observed business cycles in which output, consumption, investment, hours worked, and the real wage all rise and fall together. This lack of comovement is clearly problematic in viewing investment shocks as the dominant source of business cycle fluctuations. In this paper, we resolve the comovement problem by extending the standard neoclassical sticky-price model to a twosector model with consumer durable services.

There is a growing volume of literature that studies consumer durable services. Mankiw (1985) stated the importance of understanding fluctuations in consumer durable services for understanding economic fluctuations in a paper that empirically estimated the link between interest rates and consumer durable services. Baxter (1996) formally established a theoretical model with two sectors that

<sup>&</sup>lt;sup>1</sup> Section 2 offers the evidence of comovement between consumption and investment in response to positive investment shocks.

produce nondurable goods for consumption and durable goods for investment in consumer durable services and two types of capital. She investigated the effects of single shocks and sectoral shocks to Solow residuals on business cycles. Recently, there has been a growing literature led by Barsky et al. (2003, 2007) that studied sticky-price models with two sectors that produced nondurable goods for consumption and durable goods for consumer durable services (e.g., Monacelli, 2009; Carlstrom and Fuerst, 2010; Bouakez et al., 2011; Sudo, 2012). This literature envisaged the effects of monetary policy shocks upon business cycles. Our study extends the strand of the research by incorporating consumer durable services in order to study the effects of capital investment-specific shocks on business cycle fluctuations.

Like Baxter (1996) and Barsky et al. (2003, 2007), our model includes two sectors that produce nondurable goods and durable goods. Nondurable goods are used for consumption, and durable goods are used for investment in capital and consumer durable services. The household obtains utility from consuming nondurable goods and consumer durable services. As in Barsky et al. (2003, 2007), nondurable prices are stickier than durable prices.<sup>2</sup> Like Greenwood et al. (1997, 2000), there is a technical change specific to capital investment. If there were no consumer durable services, our twosector sticky-price model would behave like a one-sector sticky-price model. In such a model, a positive capital investment-specific shock increases the efficiency of capital accumulation. An increase in the efficiency of capital investment creates an intertemporal substitution effect which dominates the income effect so that current nondurable consumption is substituted away toward investment and thus future consumption. Hence, there is the comovement problem. By contrast, because our two-sector model has consumer durable services, an additional effect is created. A positive capital investment-specific shock decreases the real price of capital (i.e., Tobin's Q), which raises the demand for capital investment. An increase in the demand for capital investment raises the price of durable goods relative to nondurables. This generates an intratemporal substitution effect away from consumer durable services and toward nondurable consumption that dominates the intertemporal substitution effect. As a result, nondurable consumption rises, and the comovement problem is resolved.

We note that if consumer durable services were introduced in a one-sector model, the comovement problem could not be resolved because there would not be an endogenous price of durables relative to nondurables. Indeed, Justiniano et al. (2010, Table 2) considered an extension of their baseline model to one with consumer durable services. In their extension, the household allocated income flows to nondurable consumption, capital investment and consumer durable investment. Even

 $<sup>^2</sup>$  Bils and Klenow (2004) have documented that the price of durable goods changes more frequently than that of consumption goods.

though there were sticky prices of intermediates, there was only one final goods price. Without an endogenous price of durables relative to nondurables, there is no *intratemporal* substitution effect away from consumer durable services and toward nondurable consumption. As a consequence, the comovement problem is not resolved.

For related literature studying capital investment shocks, Guerrieri et al. (2014) is the closest model to ours in that it is a two-sector model. These authors extended the one-sector model of Greenwood et al. (1997) to two sectors that produce machinery and nonmachinery goods, which are in turn used to assemble three types of final goods: equipment investment, structures investment and nondurable consumption. They resolved the comovement problem by studying multifactor productivity (MFP) shocks to the machinery sector in place of shocks to the marginal efficiency of investment (MEI). They found that the MFP shock increases consumption because of a weaker intertemporal substitution effect and a stronger wealth effect due to incomplete sectoral specialization in producing final goods, whereas the MEI shock temporarily decreases consumption substantially and creates the comovement problem. Unlike their paper, in our paper the MEI shock does not have the comovement problem, due to an intratemporal substitution effect which dominates the intertemporal substitution effect. In particular, nondurable consumption follows a hump shape in our model, which is consistent with the data, as opposed to changes in consumption with a U shape in response to the MFP shock in their model.

Moreover, our study complements three other papers that attempted to resolve the comovement problem using one-sector models with variable capital utilization. First, Kahn and Tsoukalas (2011) studied a sticky price-wage model with the cost of capital utilization in terms of a higher depreciation rate of capital and with nonseparable preferences with a zero wealth effect on labor supply. By increasing the marginal productivity of labor, a higher utilization rate generated a substitution effect away from leisure and toward consumption, and resolved the comovement problem. Next, Eusepi and Preston (2009) also studied a model with the cost of capital utilization in terms of a higher depreciation rate of capital. They found that the heterogeneity in labor supply and consumption of employed and unemployed workers can generate comovement in response to investment shocks, since individual consumption was affected by the number of hours worked with the employed consuming more on average than the unemployed, and changes in the employment rate then affect aggregate consumption. Finally, Furlanetto and Seneca (2010) envisaged a model with the cost of capital utilization in terms of the maintenance cost of capital. They resolved the comovement problem by combining variable capacity utilization with nominal rigidities (in prices and wages) and nonseparable preferences with a zero wealth effect on labor supply. Unlike these papers, the mechanism in our paper is to consider consumer durable services so that there is an intratemporal substitution effect which dominates the intertemporal substitution effect.

The remainder of this paper is organized as follows. In Section 2, we present empirical evidence of comovement between consumption and investment in response to capital investment-specific shocks. In Section 3, we set up basic sticky-price models with and without consumer durable services. In Section 4, we calibrate the models and envisage the impulse responses to a positive capital investment-specific shock. Section 5 is the sensitivity analysis. Finally, concluding remarks are offered in Section 6.

#### 2. Investment shocks and comovement: empirical evidence

This section estimates a vector autoregression (VAR) model, and offers evidence showing that consumption and investment comove in response to investment shocks. Fisher (2006) has utilized a VAR model to estimate the impulse responses of the investment price, labor productivity, hours and output to capital investment shocks. Here, we follow his approach to estimate the impulse responses of consumption, investment and other variables to capital investment shocks.<sup>3</sup> We will find the evidence of comovement between consumption and investment in response to capital investment shocks. The evidence complements the findings provided by Fisher (2006).

To this end, we formulate a 7-variable VAR representation for the US economy written as

$$\mathbf{y}_t = \mathbf{\Gamma} \mathbf{y}_{t-1} + \mathbf{\Pi} \mathbf{u}_t, \tag{1}$$

where  $\mathbf{u}_t$  is a vector of structural disturbances, and  $\mathbf{\Gamma}$  and  $\mathbf{\Pi}$  are matrices to be estimated.<sup>4</sup> The vector  $\mathbf{y}_t$  consists of seven variables that include real gross domestic product (GDP), real consumption, real investment, hours, real wages, real consumer durable investment, and the level of investment-specific technology. Following Kydland and Prescott (1990) and Del Negro et al. (2007), consumption corresponds to personal consumption expenditures on nondurables and services, while investment is the sum of gross private domestic investment and personal consumption expenditures on durables. Hours are nonfarm business hours of all persons, wages are compensation of employees in wages and salary accruals, and real consumer durable investment is personal consumption expenditures on durables. For the exogenous level of capital investment-specific technology,<sup>5</sup> we follow Fisher's (2006)

<sup>&</sup>lt;sup>3</sup> Different from Fisher (2006), our model does not involve a trend in the level of productivity. As a result, our model only assumes short-run recursive restrictions, without imposing long-run identifying restrictions.

<sup>&</sup>lt;sup>4</sup> Following Hamilton (1994), we impose the restrictions that the matrix  $\mathbf{\Pi}$  be lower triangular, and the structural disturbances in  $\mathbf{u}_t$  be serially uncorrelated and uncorrelated with each other.

<sup>&</sup>lt;sup>5</sup> Our model below includes the sector producing nondurable consumption and the sector producing investment goods for capital and consumer durables. However, there are no data for the technology level of capital

method and use the inverse of the real price of capital to measure the level of investment-specific technology. Finally, to measure the real price of capital, we also follow Fisher's (2006) method, which is based on Gordon (1990) and Cummins and Violante (2002), and construct the (quality-adjusted) real price of equipment capital and software by dividing the equipment and software deflator by the consumption deflator. The source of the data is the Federal Reserve Economic Data, published by the Federal Reserve Bank of St. Louis, over the period 1947:Q1–2011:Q4.<sup>6</sup> The quarterly data are seasonally adjusted, deflated by the GDP deflators, and expressed in logarithms.

We use ordinary least squares to estimate this VAR model with an optimal lag length of two selected by the Akaike information criterion (AIC).<sup>7</sup> To recover the parameters in the structural VAR, we carry out a Cholesky decomposition of the residuals of the VAR. The ordering of the variables is real GDP, real consumption, real investment, hours, real wages, real consumer durable investment, and the level of investment-specific technology.<sup>8</sup> The ordering helps illustrate the stylized evidence of the comovement between consumption and investment in response to an investment-specific technology shock so as to motivate the purpose of our model in this paper.

We compute the impulse response functions (IRFs) to a one-standard-deviation innovation to the level of investment-specific technology. We also construct the approximate 95-percent confidence bands (two standard errors) for each IRF using 500 Monte Carlo repetitions. Figure 1 presents estimated IRFs of GDP, consumption, investment and other variables with 95-percent confidence bands illustrated by dashed lines.

#### [Insert Figure 1 here]

As is clear from the figure, a one-standard-deviation increase in the level of capital investmentspecific technology causes a rise in all variables on impact. GDP, hours and wages all increase. In particular, Panels B and C indicate that consumption and aggregate investment both increase on impact in response to investment-specific technology shocks. This offers the evidence that consumption and investment comove in response to investment shocks. Our results also show that consumer durable

investment goods. As a result, we follow Fisher's measure.

<sup>&</sup>lt;sup>6</sup> We employ 2011:Q4 as the end period because the data of the equipment and software deflator end in 2011:Q4. This series was discontinued afterward, and in the new NIPA data, equipment and software are classified as two separated series.

<sup>&</sup>lt;sup>7</sup> The optimal lag length selected by the Schwarz information criterion (SC) is one. We choose a longer optimal lag length of two quarters in order to capture more dynamics.

<sup>&</sup>lt;sup>8</sup> We follow the Cholesky decomposition of the VAR used by Bernanke et al. (1999), Christiano et al. (1997), Erceg and Levin (2006), Galí (2008), and Monacelli (2009), wherein these authors selected an ordering such that the impulse variable (the federal funds rate) is placed in the last. That means the impulse variable does not affect the remaining variables contemporaneously but can affect them with a lag. In our VAR, alternative orderings yield the robust results, as long as the level of investment-specific technology is not put in the first.

investment displays an opposite path to other variables in initial periods (cf. Panel F). Moreover, as we use the inverse of the real price of capital to measure the level of investment-specific technology, a rise in the level of investment-specific technology is associated with a fall in the real price of capital, and thus, a fall in Tobin's Q (cf. Panel G).

#### 3. Two-sector sticky-price models with and without consumer durable services

Two neoclassical sticky-price models are analyzed. One model includes consumer durable services and the other model does not. The model without consumer durable services is a special case of the model with consumer durable services.

The economy includes two final goods sectors: the nondurable goods and the durable goods sectors. The nondurable goods sector produces goods for nondurable consumption. The durable goods sector produces goods for two types of investment: investment in capital and investment in consumer durable services.<sup>9</sup> Each sector has a continuum of firms which produce and sell final goods at competitive prices and a continuum of businesses which produce and sell intermediates at monopolistic prices. The economy also consists of a continuum of households that supply labor elastically, consume, and offer capital. As the nondurable goods sector produces goods only for consumption, it is also referred to as the consumption goods sector. Similarly, the durable goods sector produces goods for investment and is also referred to as the investment goods sector. We use subscripts j=C, I to denote the consumption goods and the investment goods sectors, respectively.

#### 3.1 Final Goods Producers

In each sector, there is a continuum of *final goods* producers of a unit mass. The representative producer in sector j=C, I, produces  $Y_j$  by combining a continuum of intermediates  $Y_{jt}(z)$ ,  $z \in [0, 1]$ , according to the following technology:

$$Y_{jt} = \left[\int_{0}^{1} (Y_{jt}(z))^{(\varepsilon_{j}-1)/\varepsilon_{j}} dz\right]^{\varepsilon_{j}/(\varepsilon_{j}-1)}, \ j=C, \ I,$$
(2a)

where  $\varepsilon_j > 1$  is the elasticity of substitution between intermediates. Nondurable goods  $Y_C$  are used for consumption. Durable goods  $Y_I$  are used for both capital investment  $I_K$  and consumer durable investment  $I_D$  which form the stock of capital and the stock of consumer durables, respectively. Final goods markets are competitive. The laws of motion for capital and consumer durable services will be

<sup>&</sup>lt;sup>9</sup> As in Baxter (1996), purchases of new consumer durables come from the sector producing investment goods. See also Kydland and Prescott (1990), Cooley and Prescott (1995), Christiano et al. (2005) and Del Negro et al. (2007).

specified in the household's problem below.

Maximization of profits in sector *j* gives the demand for the intermediate *z* in sector *j*:

$$Y_{jt}(z) = \left(\frac{P_{jt}(z)}{P_{jt}}\right)^{-\varepsilon_j} Y_{jt}, \ z \in [0, \ 1], \ j = C, \ I,$$
(2b)

where  $P_{Cl}$  is the price of consumption (or nondurable) goods,  $P_{ll}$  is the price of investment (or durable) goods and  $P_{il}(z)$  is the price of the intermediate z in sector j.

A zero profit of final goods gives the following price of final goods in sector *j*.

$$P_{jt} = \left[\int_{0}^{1} (P_{jt}(z))^{1-\varepsilon_{j}} dz\right]^{1/(1-\varepsilon_{j})}, \ j = C, \ I.$$
(2c)

#### 3.2 Intermediate Goods Producers

In each sector, there is a continuum of *intermediate producers* of a unit mass indexed by  $z \in [0, 1]$ . The representative producer rents capital and hires labor to produce intermediates according to the following technology:

$$Y_{jt}(z) = A_j K_{jt}(z)^{\alpha_j} L_{jt}(z)^{1-\alpha_j}, \quad j = C, \ I,$$
(3a)

where  $K_{jt}(z)$  is capital and  $L_{jt}(z)$  is labor employed by a producer z in sector j. The parameter  $\alpha_j \in (0, 1)$  is the capital share and  $A_j > 0$  is a productivity coefficient in sector j.

A producer z in sector j sells intermediates to final goods producers in sector j at a monopolistic price. In setting a price  $P_{jt}(z)$ , we follow Rotemberg (1982) and assume that an intermediate producer z faces the following adjustment cost:

$$\Theta(P_{jt}(z)) = \frac{\theta_j}{2} (\frac{P_{jt}(z)}{P_{jt-1}(z)} - 1)^2 P_{jt} Y_{jt}, \quad j = C, \ I,$$
(3b)

where  $\vartheta_j$  measures the degree of nominal rigidities in sector *j*.<sup>10</sup>

In each period, the firm z decides how much labor to hire, how much capital to rent and what prices to set. Managers of the firm maximize the value to the owners which is the present discounted value of all current and future expected cash flows.

$$E_0 \sum_{t=0}^{\infty} \frac{\beta^t A_t}{A_0} [P_{jt}(z) Y_{jt}(z) - W_t L_{jt}(z) - R_t K_{jt}(z) - \Theta(P_{jt}(z))], \ j = C, \ I,$$
(4)

where  $W_t$  is the nominal wage and  $R_t$  is the nominal capital rental, with their small cases denoting the real wage and the real capital rental in terms of consumption goods, respectively (i.e.,  $w_t \equiv W_t/P_{Ct}$  and  $r_t \equiv R_t/P_{Ct}$ ). In (4),  $E_t$  is conditional expectations in any given period t, and  $\frac{\beta' A_t}{A_0}$  is the stochastic

<sup>&</sup>lt;sup>10</sup> An alternative method of price adjustment is random price durations based on Calvo (1983). According to Rotemberg (1987), Roberts (1995) and Galí (2008), these two methods generate the same inflation dynamics.

discount factor, with  $\beta \in (0, 1)$  and  $\Lambda_t$  being, respectively, the discount factor and the period-*t* marginal utility of real income of the representative household that owns the firm. As will be clear below, the period-*t* stochastic discount factor is equal to the owner's marginal rate of substitution between period *t* and period 0.

Given the technology (3a), managers choose  $\{L_{jt}(z), K_{jt}(z), P_{jt}(z)\}_{t=0}^{\infty}$  to maximize the cash flows in (4) subject to the demand for the intermediate *z* in (2b). Let  $\lambda_{jt}(z)$  denote the current-valued Lagrange multiplier of the demand for the intermediate *z* in (2b), *j*=*C*, *I*. Moreover, denote  $MP_{jt}^{L}(z)$  and  $MP_{jt}^{K}(z)$ as the period-*t* marginal product of labor and capital for the intermediate firm *z* in sector *j*, respectively. The first-order conditions for  $L_{jt}(z)$ ,  $K_{jt}(z)$  and  $P_{jt}(z)$  are

$$w_t = \lambda_{jt}(z) \frac{P_{jt}(z)}{P_{Ct}} M P_{jt}^L(z), \qquad (5a)$$

$$r_t = \lambda_{jt}(z) \frac{P_{jt}(z)}{P_{Ct}} M P_{jt}^K(z),$$
(5b)

$$\left\{ \left[ 1 - (1 - \lambda_{jt}(z)) \mathcal{E}_{j} \right] \left( \frac{P_{jt}(z)}{P_{jt}} \right)^{-\mathcal{E}_{j}} - \mathcal{G}_{j}(\pi_{jt}(z) - 1) \frac{P_{jt}}{P_{jt-1}(z)} + \lambda_{jt}(z) \left[ \frac{Y_{jt}(z)}{Y_{jt}} - \left( \frac{P_{jt}(z)}{P_{jt}} \right)^{-\mathcal{E}_{j}} \right] \right\} Y_{jt} + E_{t} \left[ \frac{\beta A_{t+1}}{A} \mathcal{G}_{j}(\pi_{jt+1}(z) - 1) \frac{\pi_{jt+1}(z)}{\pi_{Q+1}} \frac{P_{jt+1}}{P_{jt}(z)} Y_{jt+1} \right] = 0, \quad (5c)$$

where  $\pi_{jl}(z) \equiv P_{jl}(z)/P_{jl-1}(z)$  is the gross inflation of the intermediate *z* in sector *j*.

By imposing the symmetry conditions of  $K_{jt}(z)=K_{jt}$ ,  $L_{jt}(z)=L_{jt}$ ,  $P_{jt}(z)=P_{jt}$ ,  $Y_{jt}(z)=Y_{jt}$  and  $\lambda_{jt}(z)=\lambda_{jt}$ for all z, (5a)-(5c) give, respectively,

$$\frac{w_t}{\lambda_{jt}} = \frac{P_{jt}}{P_{Ct}} M P_{jt}^L, \quad j = C, \quad I,$$
(6a)

$$\frac{r_t}{\lambda_{jt}} = \frac{P_{jt}}{P_{Ct}} M P_{jt}^K, \quad j = C, \quad I,$$
(6b)

$$\frac{1}{\lambda_{jt}} = \frac{\varepsilon_j}{\varepsilon_j - \Omega_{jt}}, \quad j = C, \quad I,$$
(6c)

where  $\Omega_{jt} \equiv 1 - \vartheta_j (\pi_{jt} - 1) \pi_{jt} + E_t [\frac{\beta A_{t+1}}{A_t} \vartheta_j (\pi_{jt+1} - 1) \frac{(\pi_{jt+1})^2}{\pi_{Ct+1}} \frac{Y_{jt+1}}{Y_{jt}}], j = C, I.$ 

The multiplier  $\lambda_{jt}$  stands for the real marginal cost of intermediates in sector *j* in period *t*, and its inverse in (6c) is the markup over the marginal cost. Thus, in (6a), the demand for labor is determined by the markup over the real wage equal to the real marginal product of labor. Similarly, in (6b), the demand for capital is determined by the markup over the real rental equal to the real marginal product of capital.

Data indicate that durable prices are more flexible than nondurable prices (cf. Bils and Klenow, 2004). To simplify the analysis, our baseline analysis will focus on the case wherein durable prices are flexible and nondurable prices are sticky. For robustness, we will also carry out analyses of the case where durable prices are sticky but less so than nondurable prices. Note that a flexible durable price

gives  $\mathcal{G}_I=0$ , and thus  $\Omega_{It}=1$  for all *t*. In this case, the markup  $1/\lambda_{It}=\varepsilon_I/(\varepsilon_I-1)$  is constant for all *t*. Moreover, in a steady state,  $\pi_{jt}=\pi_{jt+1}=1$  for j=C, *I*, so  $\Omega_{jt}=\Omega_{jt+1}=1$ . Then, the markup is  $1/\lambda_j=\varepsilon_j/(\varepsilon_j-1)$  in a steady state for j=C, *I*.

#### 3.3 Households

Households obtain utility from nondurable consumption and consumer durable services and encounter disutility from working. Following Baxter (1996) and Barsky et al. (2003, 2007), we define an index of consumption X as a function of consumption and consumer durable services given as follows.

$$X_{t} \equiv \left[ \left( 1 - \mu \right)^{\frac{1}{\eta}} \left( C_{t} \right)^{1 - \frac{1}{\eta}} + \mu^{\frac{1}{\eta}} \left( D_{t} \right)^{1 - \frac{1}{\eta}} \right]^{\frac{\eta}{\eta - 1}}, \tag{7a}$$

where  $C_t$  is consumption and  $D_t$  is the stock of consumer durables which offers services to the household in period *t*. The parameter  $\mu > 0$  is the share of consumer durable services, and  $\eta \ge 0$  is the elasticity of substitution between consumption and consumer durable services.

The household's expected lifetime utility is

$$E_{0}\left\{\sum_{t=0}^{\infty} (\beta)^{t} \left(\log X_{t} - \nu \frac{(L_{t})^{1+\phi}}{1+\phi}\right)\right\},$$
(7b)

where  $L_t$  is the hours of work. The parameter  $\nu > 0$  is the coefficient associated with the disutility of work, and  $\phi > 0$  is the inverse of the Frisch labor supply elasticity. The instantaneous utility in (7b) is separable with the logarithmic form for the index of consumption. The utility function is consistent with the balanced growth path (cf. King and Rebelo, 1999).

In each period *t*, the representative household faces the following budget constraint:

$$C_{t} + p_{t}(I_{Kt} + I_{Dt}) + b_{t} = i_{t-1}\frac{b_{t-1}}{\pi_{Ct}} + r_{t}K_{t} + w_{t}L_{t} + \frac{T_{t}}{P_{Ct}} + \frac{F_{t}}{P_{Ct}},$$
(8)

where  $p_t \equiv P_{tt}/P_{Ct}$  is the relative price of durables.  $K_t$  is capital holding at the beginning of period t, and  $B_{t-1}$  is nominal bond holdings at the end of period t-1, with  $b_{t-1} \equiv B_{t-1}/P_{Ct-1}$  being its real value.  $i_{t-1}$  is the gross nominal interest rate on a bond holding between t-1 and t.  $T_t$  is nominal lump-sum transfers, and  $F_t$  is nominal profits remitted from firms (i.e., dividends) in t. Thus, in each period t, with real income flows from returns to bonds and capital, wages, lump-sum transfers and dividends, the household chooses consumption, labor supply, capital investment, consumer durable investment and bond holdings.

The stock of consumer durables can be produced from investment goods on a one-to-one basis net of adjustment costs. The stock of consumer durables evolves according to

$$D_{t} - (1 - \delta_{D})D_{t-1} = [1 - \Phi_{D}(\frac{I_{Dt}}{I_{Dt-1}})]I_{Dt}, \qquad (9a)$$

where  $0 < \delta_D < 1$  is the depreciation rate of the stock of consumer durables and the function  $\Phi_D(.)$  is the fraction of adjustment cost of investment in consumer durables.

The story for capital investment is different. The accumulation equation for the stock of capital is expressed as

$$K_{t+1} - (1 - \delta_K) K_t = \xi_t [1 - \Phi_K (\frac{I_{Kt}}{I_{Kt-1}})] I_{Kt},$$
(9b)

where  $0 < \delta_K < 1$  is the depreciation rate of capital and the function  $\Phi_K$  is the fraction of adjustment costs in capital investment. Note that we follow Greenwood et al. (1997, 2000) and Justiniano et al. (2010) and include a factor  $\xi_t$  in the accumulation of capital in (9b). The factor  $\xi_t$  represents the current state of the technology for forming capital. It is an exogenous variation in efficiency and determines the amount of capital in the next period that can be formed from one unit of investment goods in this period. Changes in  $\xi_t$  formalize the notion of capital investment-specific technological change.

Following Christiano et al. (2005) and Justiniano et al. (2010), we assume that the function of the adjustment cost  $\Phi_i$  takes the form  $\Phi_i(\frac{I_u}{I_{u-1}}) = \frac{\varphi_i}{2}(\frac{I_u}{I_{u-1}}-1)^2$ ,  $\varphi_i \ge 0$ , i=D, K.<sup>11</sup>

As in existing work on capital investment-specific technology shocks, we assume that  $\xi_i$  follows a first-order stochastic process.

$$\log \xi_t = \rho \log \xi_{t-1} + e_t, \tag{10}$$

where the innovation in relation to the capital investment shock  $e_t$  is assumed to be independent and identically distributed normally, with mean 0 and variance  $\sigma^2$ .

Several remarks are in order. As is standard, capital investment is accumulated into the stock of capital in the next period in (9b), and thus capital investment is for use in production in the next period. On the other hand, in terms of value, we think of consumer durables as mainly from residential houses. When these consumer durables are purchased, they are ready for use as consumption services. Hence, in (9a) we follow the conventional wisdom in Barsky et al. (2003, 2007), Monacelli (2009) and Sudo (2012) and posit that the flow of consumer durables forms the stock in the same period.

Second, we posit that only capital investment has investment shocks, because when both investments are subject to investment shocks, the intratemporal substitution effect is so weak that it cannot dominate the intertemporal substitution effect. Then, the comovement problem cannot be resolved. Our formulation is based on the following reasons. First, in Greenwood et al. (1997, 2000), there are two types of capital that are accumulated from investment that is produced in the same sector, but only equipment capital has investment-specific technology shocks while structures capital is not

<sup>&</sup>lt;sup>11</sup> The form gives  $\Phi'_i(\frac{I_i}{I_{i-1}}) = \varphi_i(\frac{I_{ii}}{I_{ii-1}}-1)$  and  $\Phi'_i(\frac{I_{ii+1}}{I_{ii}}) = \varphi_i(\frac{I_{ii+1}}{I_{ii}}-1).$ 

affected by investment-specific technology shocks. Second, and more importantly, existing studies, such as Chung, Kiley and Laforte (2010), argue that there are two categories of durables, and they differ in the way they are affected by investment-specific shocks. The first category of durables includes personal computers and home appliances. It is likely that production of these goods receives a favorable impact from a positive investment technology shock. The second category of durables includes residential investments. Existing studies agree that productivity of residential investment is not affected by investment-specific technology shocks. In terms of value, the majority of consumer durables are residential houses. Thus, we can think of consumer durables in our paper as residential houses, and their productivity is not affected by investment-specific technology shocks.

Moreover, viewing consumer durables as residential housing, our formulation is the same as Barsky et al. (2003), whose model includes two sectors: a durable goods sector and a nondurable goods sector. In Barsky et al. (2003, Section 6), their specification allows for the durable to function as productive capital or consumer durables, the former of which is treated as fixed. Thus, our two-sector model is similar to that of Barsky et al. (2003), except that our model allows for capital accumulation and investment-specific technology shocks, and their model does not.<sup>12</sup>

Furthermore, although like Barsky et al. (2003), investment in both capital and consumer durables comes from the same sector and thus has the same good price  $p_{It}$ , capital investment is subject to an investment-specific technology progress at rate  $\xi_t$ , and consumer durable investment is not. As a result, the price of capital investment relative to the price of consumer durable investment is not unity but is  $1/\xi_t$ , which is Tobin's Q. When the investment-specific shock follows the first-order stochastic process as in (10), their relative price also follows a stochastic process.

The representative household's problem is to maximize the expected lifetime utility (7b) subject to (8), (9a) and (9b). Let  $\Lambda_t$ ,  $\zeta_t$ , and  $q_t$  be the current-valued Lagrange multipliers of the budget constraint (8), the accumulation of consumer durables (9a), and the capital accumulation equation (9b), respectively. Moreover, we denote  $U_{Ct}$ ,  $U_{Dt}$  and  $U_{Lt}$ , respectively, as the marginal utility of consumption, consumer durable services and hours worked in *t*. The first-order conditions for  $C_t$ ,  $L_t$ ,  $b_t$ ,  $I_{Kt}$ ,  $I_{Dt}$ ,  $K_{t+1}$ and  $D_t$  are

<sup>&</sup>lt;sup>12</sup> The purpose of Barsky et al. (2003, 2007) is to study the business-cycle effect of a monetary shock, not an investment shock. In particular, these authors found a comovement problem because, in response to monetary tightening, non-durable consumption decreases but consumption durables increase. Monacelli (2009) allowed for friction in lending between households in the model of Barsky et al. (2003, 2007) and resolved the comovement problem only when durable prices have some degrees of stickiness. The comovement puzzle is not settled when durable prices are flexible. By adding capital into the model of Monacelli (2009), Chen and Liao (2014) resolved the comovement problem when durable prices are flexible.

$$U_{Ct} = \Lambda_t, \tag{11a}$$

$$\frac{-U_{li}}{U_{ci}} = w_l, \tag{11b}$$

$$U_{Ct} = \beta E_t \left( U_{Ct+1} \frac{i_t}{\pi_{Ct+1}} \right), \tag{11c}$$

$$p_{t}U_{Ct} = p_{t}q_{t}\xi_{t} \left[ 1 - \Phi_{K}\left(\frac{I_{Kt}}{I_{Kt-1}}\right) - \frac{I_{Kt}}{I_{Kt-1}}\Phi_{K}'\left(\frac{I_{Kt}}{I_{Kt-1}}\right) \right] + \beta E_{t} \left[ p_{t+1}q_{t+1}\xi_{t+1}\left(\frac{I_{Kt+1}}{I_{Kt}}\right)^{2}\Phi_{K}'\left(\frac{I_{Kt+1}}{I_{Kt}}\right) \right], \quad (11d)$$

$$p_{t}U_{Ct} = p_{t}\zeta_{t} \left[ 1 - \Phi_{D}(\frac{I_{Dt}}{I_{Dt-1}}) - \frac{I_{Dt}}{I_{Dt-1}} \Phi_{D}'(\frac{I_{Dt}}{I_{Dt-1}}) \right] + \beta E_{t} \left[ p_{t+1}\zeta_{t+1}(\frac{I_{Dt+1}}{I_{Dt}})^{2} \Phi_{D}'(\frac{I_{Dt+1}}{I_{Dt}}) \right],$$
(11e)

$$p_{t}q_{t} = \beta E_{t} \left[ r_{t+1}U_{Ct+1} + p_{t+1}q_{t+1}(1 - \delta_{K}) \right],$$
(11f)

$$p_{t}\zeta_{t} = U_{Dt} + \beta E_{t} \left[ p_{t+1}\zeta_{t+1} (1 - \delta_{D}) \right],$$
(11g)

along with the transversality conditions  $\lim_{t\to\infty}(\beta)^t \Lambda_t b_t = 0$ ,  $\lim_{t\to\infty}(\beta)^t q_t K_{t+1} = 0$  and  $\lim_{t\to\infty}(\beta)^t \zeta_t D_t = 0$ . Thus,  $\Lambda_t$  is the marginal utility of the household. Using (11a), the firm's stochastic discount factor  $\frac{\beta^t \Lambda_t}{\Lambda_0}$  in (4) is equal to  $\frac{\beta^t U_{\Omega}}{U_{C0}}$ , which is the intertemporal marginal rate of substitution between period *t* and period 0.

In these conditions, (11a) and (11b) are standard, and (11c) is the consumption-Euler equation, which equates the marginal utility of consumption in this period to the discounted expected marginal utility of shifting one unit of consumption to the next period. In condition (11d),  $q_t$  is the shadow value of installed physical capital. Like Justiniano et al. (2010), Tobin's Q is  $\frac{q_t}{A}$ , the relative marginal value of installed capital with respect to consumption, which is the real price of capital stock. This condition equates the foregone value of capital investment, which is the marginal utility of consumption, to the marginal value of capital investment. The marginal value of capital investment includes the shadow value, net of adjustment costs, of installed physical capital in this period (the first term) and the enhanced shadow value of capital due to lowering adjustment costs in the next period (the second term). In the case without adjustment costs of capital investment (i.e.  $\Phi_K=0$  and  $\Phi_K'=0$ ), the condition reduces to  $\frac{q_t}{A_t} = \frac{1}{\xi_t}$ , which indicates that, in optimum, Tobin's Q is equal to a reciprocal of capital investment shocks. It follows that positive capital investment.

Similar to (11d), condition (11e) equates the marginal utility of consumption to the marginal value of consumer durable investment. The stock of consumer durables also has a Tobin's Q-like concept which is the shadow value of consumer durable services in terms of consumption,  $\frac{\zeta_i}{A_i}$ . In the case without adjustment costs of consumable durable investment (i.e.  $\Phi_D=0$  and  $\Phi_D'=0$ ), the condition

reduces to  $\frac{\zeta_t}{A_t} = 1$ , which indicates that, in optimum, the marginal value of consumer durable services is equal to the marginal utility of consumption.

Condition (11f) determines the demand for capital in the next period. The marginal cost of capital is this period's effective relative price of durables evaluated by the shadow value of installed physical capital. The marginal benefit is the expected discounted sum of the next period's real rental (in terms of consumption) and next period's effective relative price of undepreciated capital evaluated by the shadow value of installed capital.

Finally, (11g) determines the demand for consumer durable services in this period. The marginal cost is this period's effective relative price of durables evaluated by the shadow value of consumer durable services. The marginal benefit is the sum of this period's marginal utility of consumer durable services and the expected discounted next period's effective relative price of undepreciated consumer durables evaluated by the shadow value of consumer durable services. Through (11g), variations in the relative price of durables are expected to affect the demand for nondurable consumption as analyzed in the next section.

#### 3.4 Equilibrium

In equilibrium, the consumption goods and the investment goods markets clear.

$$Y_{Ct} - \frac{g_C}{2} (\pi_{Ct} - 1)^2 Y_{Ct} = C_t, \qquad (12a)$$

$$Y_{lt} - \frac{g_l}{2} (\pi_{lt} - 1)^2 Y_{lt} = I_{Kt} + I_{Dt}.$$
 (12b)

We abstract from redistribution via the fiscal policy, and hence  $T_t=0$ . Moreover, the capital, the labor and the bond markets all clear.

$$K_t = K_{Ct} + K_{It}, (13a)$$

$$L_t = L_{Ct} + L_{It}, \tag{13b}$$

$$b_t = 0.$$
 (13c)

The model is closed by a monetary policy rule. As we do not analyze the effects of monetary shocks, the simplest rule is used.

$$\frac{i_t}{i} = \left(\frac{\pi_t}{\pi}\right)^{\chi}, \quad \chi > 1, \tag{14}$$

where  $\pi_i \equiv (\pi_{Cl})^{1-\mu} (\pi_{ll})^{\mu}$  is a composite inflation index with the weight for nondurable goods inflation being the share of nondurable consumption in the index of consumption, and *i* and  $\pi$  are steady-state values. We assume that  $\chi$  is sufficiently large in order to ensure equilibrium determinacy.

#### 3.5 The model without consumer durable services

The model without consumer durable services is a special case of the two-sector model above when there are no consumer durable services. In the model without consumer durable services, the utility function in (7b) is reduced to  $\log C_t - v(L_t)^{1+\phi}/(1+\phi)$ . Moreover, (9a), (11e), and (11g) are not equilibrium conditions. As equilibrium conditions (8) and (12b) involve consumer durable investment, they are also modified.

Even with two sectors, because of no consumer durable services, as will be seen below, a positive capital investment-specific shock leads to an increase in investment and a decrease in consumption, thus the comovement problem, as in Justiniano et al. (2010).

#### 4. Comparisons of both models

In this section, we study the effects of positive investment-specific technology shocks on the impulse responses of aggregate macro and other relevant variables.

#### 4.1 Calibration

The time frequency is quarterly. The households' discount factor  $\beta$  is pinned down by the steadystate real rate of return *i*. We choose a real rate of return per annum of 4%. This implies a quarterly discount factor of  $\beta$ =0.99.

For production, the total factor productivities in the consumption goods and investment goods sectors are normalized to unity, so  $A_C=A_I=1$ . We follow Acemoglu and Guerrieri (2008) and set the capital shares of the investment goods and the consumption goods sectors equal to  $\alpha_I=0.27$  and  $\alpha_C=0.47$ , respectively, to match the average capital shares in their respective sectors between 1987 and 2005. The elasticity of substitution between intermediates is set so that the desired markup is 20% in both sectors which gives  $\varepsilon_C = \varepsilon_I = 6$ . We follow Hansen (1985) and set the quarterly depreciation rate of capital equal to  $\delta_K=0.025$ , which implies a 10% annual depreciation rate. Moreover, following Carlstrom and Fuerst (2010) and Sudo (2012), we assume that the quarterly depreciation rate for consumer durable services equals  $\delta_D=0.025$ .<sup>13</sup>

As to the coefficient of adjustment costs, the existing literature sets a zero adjustment cost for the accumulation in consumer durable investment (e.g., Iacoviello, 2005; Barsky et al., 2007; Monacelli, 2009). We follow this convention and set  $\varphi_D=0$ . We set the coefficient of adjustment costs in capital investment to be  $\varphi_K=0.5\%$ . This value is somewhat smaller than the value used by Greenwood et al.

<sup>&</sup>lt;sup>13</sup> Our results are robust within a wide range of  $\delta_K \in [0.015, 0.055]$  and  $\delta_D \in [0.010, 0.037]$ .

(2000) and Guerrieri et al. (2014). These authors studied investment shocks in models wherein the intertemporal substitution effect dominates the income effect, which causes the comovement problem. When they use a large fraction of adjustment costs in capital investment, the intertemporal substitution effect is weakened and smaller than the income effect, so the comovement problem is resolved. By contrast, capital adjustment costs do not play such an important role in our model because, by introducing consumer durable services, there is a sufficiently large intratemporal substitution effect that dominates the intertemporal substitution effect. In order to highlight the role of consumer durable services in resolving the comovement problem, we choose a small fraction of adjustment costs in capital investment.

For the preference, by using the consumption-leisure tradeoff condition in (11b), we set the parameter value of leisure in preference at v=5.573 to target hours of work in the steady state at L=1/3. As for the elasticity of substitution between nondurable consumption and consumer durable services, we follow Barsky et al. (2007) and set  $\eta=1$ , implying a Cobb-Douglas form for the consumption index. In addition, like Barsky et al. (2007), we set the inverse of the Frisch labor supply elasticity at  $\phi=1$ , which is within the range of values used in the existing literature. We will perform robustness analysis for different values of  $\eta$  and  $\phi$  in Section 5. We choose the share of consumer durable services in the consumption index equal to  $\mu=0.2$  in order to match the 20% share of spending on consumer durables in total private spending in the US.

As for the degree of price-stickiness, we set  $\vartheta_I=0$  so that durable prices are flexible, as shown in Bils and Klenow (2004), among others. Justiniano et al. (2010) estimated the price-stickiness of consumption goods at over six quarters (the probability of not resetting prices being 0.84), and Khan and Tsoukalas (2011) estimated the price-stickiness of consumption goods at over four quarters (the probability of not resetting prices being 0.77). We target the stickiness of nondurable prices at five quarters, which lies within the range of these estimates. This pins down  $\vartheta_C=96.154.^{14}$  As for the monetary policy rule, we set the coefficient of the inflation in the policy rule at  $\chi=1.5$ , which is a standard value in the literature regarding Taylor rules.

Finally, the autocorrelation of the capital investment shock and the standard deviation of errors to the capital investment shock are set to be  $\rho=0.72$  and  $\sigma=0.0603$ , respectively, which are within the

<sup>&</sup>lt;sup>14</sup> To obtain the value of  $\vartheta_C$ , we use the log-linearization of the optimal pricing condition in (6c) to yield the slope of the Phillips curve equal to  $(\varepsilon_C - 1)/\vartheta_C$ . Then, we equate the slope to the slope of the New Keynesian Phillips curve in the standard Calvo-Yun model, which is  $(1-\theta_C)(1-\beta\theta_C)/\theta_C$ , where  $\theta_C$  is the probability of not resetting prices for consumption goods. Thus, we obtain  $\vartheta_C = (\varepsilon_C - 1)\theta_C/[(1-\theta_C)(1-\beta\theta_C)]$ . See the Appendix for details. By setting the stickiness of nondurable prices at five quarters so  $1-\theta_C=1/5$ , with  $\varepsilon_C=6$  and  $\beta=0.99$ , we obtain  $\vartheta_C=96.154$ .

range of the estimated values in the literature, such as Smets and Wouters (2007), Justiniano et al. (2010) and Khan and Tsoukalas (2011).

Parameter values in the baseline parameterization are summarized in Table 1. In the Table, we also list parameter values used in the model without consumer durable services wherein all parameter values are the same as those for the model with consumer durable services except for  $\mu=0$  and a different calibrated value of v.

[Insert Table 1 here]

#### 4.2 Effects of a positive investment shock

We carry out a positive capital investment shock in the same way as in Justiniano et al. (2010). Specifically, the innovation in relation to the capital investment shock  $e_t$  is increased by one standard deviation in the stochastic process with the initial value of the capital investment shock  $\xi_t$  normalized at unity. The results of the impulse responses are illustrated in Figure 2. An increase in  $e_t$  raises the marginal efficiency of capital investment. As a result of a positive shock to the marginal efficiency of capital investment. As a result of capital goes down (cf. Panel J), which raises the demand for investment goods on impact (cf. Panel C). Since durable prices are more flexible than nondurable prices, the relative price of durables, and thus the relative price of investment, increases (cf. Panel G). A higher durable price increases inflation, which in turn raises the nominal interest rate (cf. Panel H and I). Moreover, a positive investment shock produces a drop in the price markup in sticky-price models, as is evident from the fact that the real marginal cost of intermediates in the consumption sector increases (cf. Panel F).

#### [Insert Figure 2 here]

We remark that a positive shock to the marginal efficiency of capital investment decreases the real price of capital and thus Tobin's Q. The price of capital is often seen as a good proxy for the stock market value. A positive shock to the marginal efficiency of capital investment delivers at the same time an output boom and a stock market bust, as discussed in Christiano et al. (2014).

By contrast, because we have an endogenous price of durables relative to nondurables, a positive shock to the marginal efficiency of capital investment increases the relative price of durables (i.e., the relative price of investment). A procyclical relative price of investment is consistent with the data. Although a branch of research indicated a countercyclical relative price of investment prior to the mid-1980s or 1990s (e.g., Fisher, 2006), recent evidence indicates no robust evidence that this relative price is countercyclical. For example, using three definitions of aggregate investment and two measures of the price of consumption, Beaudry et al. (2015) found that the price of investment relative to

consumption was procyclical over the post-1983 period and almost always significantly so for all the measures. When considering a longer sample, it was rarely countercyclical and never significantly so. They showed that their result held for the other G7 countries.

#### 4.2.1 The model without consumer durable services

To see the impulse responses of other variables, we begin by envisaging the effects in the model without consumer durable services. The results are delineated by the dashed red lines in Figure 2.

An increase in the marginal efficiency of capital investment generates an *intertemporal* substitution effect away from nondurable consumption and toward investment and thus future consumption. Thus, nondurable consumption falls (cf. the dashed red line in Panel B). The higher return on currently available resources would, at the same time, operate to persuade individuals to postpone leisure. Consequently, there is an expansion in hours of work and thus, output (cf. the dashed red lines in Panels D and A). Moreover, the real wage rises since the increase in the real marginal cost dominates the decrease in the marginal product of labor (cf. the dashed red line in Panel E). Therefore, all other real variables increase except for consumption. The model thus fails to generate the comovement between investment and consumption.

#### 4.2.2 The model with consumer durable services

Now, we analyze the impulse responses of other variables in the model with consumer durable services. The results are illustrated by solid blue lines in Figure 2.

Consumer durable services are now a substitute for nondurable consumption. Thus, there is another substitution effect. A higher relative price of durables generates an *intratemporal* substitution effect away from consumer durable services and toward nondurable consumption. As the intratemporal substitution effect dominates the intertemporal substitution effect, nondurable consumption goes up (cf. the solid blue line in Panel B). As a result, nondurable consumption comoves with output, investment, hours of work and real wages (cf. the solid blue lines in Panels A–E).

It should be noted that, in response to a positive capital investment shock, the model with consumer durable services amplifies the impulse responses of real variables with hump-shaped patterns (cf. the solid blue lines in Panels A–E), but the impulse responses of real variables in the model without consumer durable services do not have hump-shaped patterns (cf. the dashed red lines in Panels A–E). As remarked by King and Rebelo (1999), the results emerge because consumer durable investment has larger amplitudes of percentage fluctuations, similar to capital investment.

Furthermore, even though the consumer durable investment does not increase on impact, we have found that the consumer durable investment comoves with other real variables from t+1 onward,

because shocks to the marginal efficiency of capital investment in t influence the production of durables in t+1, which increases consumer durable investment (cf. Panel K). As a result, the simulated correlation between consumption and consumer durable investment is still positive, about 0.16.

We remark that in the figure, the maximal change of a decrease in consumer durable investment in Panel K is close to 4.8 on impact and is large as compared to the change of an increase in output in Panel A, which is near 0.1, i.e., ten percent. Nevertheless, such a large change in consumer durable investments is commonly seen in the literature on consumer durables. In the model that studied the response to a permanent one-percent increase in the money supply by Barsky et al. (2007), when nondurable prices are sticky at four quarters and durable prices are flexible as is in our model, the change of a decrease in consumer durable investment is more than 11, which magnitude is much larger than the change in output which is around 0.01. In an extension made by Monacelli (2009) later, the author introduced two types of agents, namely savers and borrowers, and found that, in response to a 25-basis-point increase in the innovation of the interest rate policy shock, the change of a decrease in consumer durable investment is much larger than the change in consumption, which is close to 0.1.<sup>15</sup>

Finally, we must report that the simulated correlation between output and consumption in our model is 0.81. The simulated correlation matches well with the correlation of 0.76 in the US over the postwar period of 1947:Q1–2016:Q2. However, in the model without consumer durable services, the simulated correlation between output and consumption is only 0.14, which fails to match the data.<sup>16</sup>

#### 4.3 Why does the model with consumer durable services resolve the comovement problem?

This subsection explains the underlying reasons why, in an otherwise standard two-sector stickyprice model with more flexible durable prices, adding consumer durable services resolves the comovement problem. At the center of the analysis is the fact that in a two-sector model with consumer durable services, the demand for consumer durable services changes the household's expenditure behavior.

First, we analyze the model without consumer durable services. By using (6a) and (11b), we obtain

$$\frac{-U_{Lt}}{U_{Ct}} = \nu L_t^{\phi} C_t = \lambda_{jt} \frac{P_{jt}}{P_{Ct}} M P_{jt}^L, \quad j = C, \quad I.$$

$$(15)$$

With standard preferences and technology, the marginal rate of substitution between consumption and leisure  $\left(\frac{-U_{Lt}}{U_{Ct}} = \nu L_t^{\phi} C_t\right)$  is increasing in consumption and hours of work, while the

<sup>&</sup>lt;sup>15</sup> These numbers are taken from Figure 1 in Barsky et al. (2007) and Figure 4 in Monacelli (2009).

<sup>&</sup>lt;sup>16</sup> When durable prices are sticky at two quarters, the simulated correlation between output and consumption is still 0.78 in our model but only 0.05 in the model without consumer durable services.

marginal product of labor  $MP_{jt}^{L}$  is decreasing in hours of work. For ease of exposition, we focus on a one-sector flexible-price model without consumer durables, so  $\lambda_{jt}=\lambda_{j}$  is constant for all t and  $P_{jt}/P_{Ct}=1$  for j=C, I. As a result, a capital investment shock that increases hours of work on impact and thus, decreases the marginal product of labor, would lower consumption in order to meet (15) in equilibrium. This is exactly what happens in response to a capital investment shock in the model without consumer durable services, as described above. A two-sector model with a consumption good sector and an investment good sector behaves like a one-sector model with goods used as consumption and investment described above. Their mechanisms are the same. As a result, consumption falls in response to a positive capital investment shock.

By contrast, in the two-sector model with consumer durables, there is an additional optimization condition which is a household's shadow value of consumer durable services in period t given by (11g) with  $\zeta_t = U_{Ct}$  when  $\varphi_D = 0$  in (11e). In the optimum, this shadow value is equal to the marginal cost of investment in consumer durable services in terms of the marginal utility of consumption. If we denote  $V_t = p_t U_{Ct}$ , the household's shadow value of consumer durable services in (11g) can be rewritten as

$$V_{t} = U_{Dt} + \beta (1 - \delta_{D}) E_{t} (V_{t+1}) = E_{t} \sum_{\tau=0}^{\infty} \beta^{\tau} (1 - \delta_{D})^{\tau} U_{Dt+\tau},$$
(16)

in which the second equality follows from the law of iterated expectations.

The condition above has something to do with the observation that the shadow value of a longlived durable is approximately unchanged in the wake of a shock (e.g., Barsky et al., 2003, 2007; House and Shapiro, 2008). This condition indicates that a household's shadow value of consumer durable services in this period is equal to the expected discounted sum of the marginal utility of undepreciated consumer durable services from period t onward. The household's shadow value of consumer durable services is quasi-constant, since variations in the flow of consumer durables in this period have little effect on the stock of consumer durables upon which the marginal utility of consumer durable services depends. With a quasi-constant shadow value of consumer durable services on the right-hand side of the second equality in (16), the relative price of durables  $p_t$  (i.e., the relative price of investment) and the marginal utility of consumption  $U_{Ct}$  in this period on the left-hand side of the first equality in (16) will move in opposite directions. A positive capital investment-specific shock decreases the real price of capital, which in turn leads to an increase in the demand for capital investment. The rise in the demand for capital investment then increases the relative price of durables. Thus, it is necessary to decrease the marginal utility of nondurable consumption, which is associated with an increase in expenditure on nondurable consumption. As a result, nondurable consumption rises, and the comovement problem is resolved.

#### 5. Sensitivity analysis

In our calibration exercises, the baseline parameter values are well justified. To better understand whether or not our results are robust to variations in key parameter values used in the baseline, this section analyzes sensitivity analysis.

#### 5.1 Price stickiness in investment goods

So far, our result of comovement is obtained under the situation wherein durable prices are flexible. Our results still hold true if durable prices are sticky but are less sticky than nondurable prices.

To see this, we carry out analysis by increasing price stickiness in investment goods. Our baseline sets  $\vartheta_I=0$  so that the probability of resetting durable prices is  $1-\theta_I=1$ . If the value of  $\vartheta_I$  is increased, the cost of durable price adjustments is higher. Then, durable prices are stickier than the baseline. With stickier durable prices, in response to a positive capital investment shock, fewer firms raise durable prices. The price of durables relative to the price of nondurables increases less than that in the baseline. Then, the intratemporal substitution effect is weaker, so consumption on impact increases by less.

Figure 3 illustrates the impulse responses when the probability of resetting durable prices  $(1-\theta_i)$  is decreased from 1 to 1/2 and then 2/5, which implies that the price of durables is reset less frequently at every 2 quarters and 2.5 quarters, respectively, with the corresponding parameter value of  $\vartheta_i$  being increased from 0 to 9.90 and then 18.47, respectively. When durable prices are adjusted less frequently, the relative price of durables is increased by a smaller degree (cf. Panel G), and thus, the intratemporal substitution effect becomes weaker. Figure 3 suggests that our result of comovement is robust even when durable prices are sticky, as long as the frequency of durable price adjustment is lower than 2.5 quarters.

#### [Insert Figure 3 here]

#### 5.2 Price stickiness in consumption goods

In our baseline, the nondurable price is reset every 5 quarters. Our results of comovement still hold true if nondurable prices are less sticky but are stickier than durable prices.

To see this, we carry out analysis by decreasing nondurable price stickiness. Our baseline sets  $\vartheta_C$ =96.15 so that the probability of resetting nondurable prices is 1- $\theta_C$ =1/5. If the value of  $\vartheta_C$  is decreased, the cost of nondurable price adjustments is lower. Then, the price of nondurable consumption is less sticky than the baseline. With less sticky nondurable prices, in response to a positive

capital investment shock, more firms raise nondurable prices.<sup>17</sup> The durable price relative to the nondurable price is not increased as much as it is in the baseline. Then, the intratemporal substitution effect is weaker, and nondurable consumption on impact is increased by less.

Figure 4 demonstrates the impulse responses when the probability of resetting nondurable prices  $(1-\theta_C)$  is increased from 1/5 to 1/4 and then 1/3.5, which implies that the consumption price is reset more frequently at every 4 quarters and 3.5 quarters, respectively, with the corresponding parameter value of  $\vartheta_C$  being decreased from 96.15 to 58.25 and then 42.68, respectively. When nondurable prices are adjusted more frequently, the relative price of durables is increased by a smaller degree (cf. Panel G), and thus, the intratemporal substitution effect becomes weaker. The figure indicates that our result of comovement is robust even when nondurable prices are less sticky, as long as the frequency of nondurable price adjustment is higher than 3.5 quarters.

#### [Insert Figure 4 here]

#### 5.3 Elasticity of substitution between consumption and consumer durable services

In our baseline, the elasticity of substitution between nondurable consumption and consumer durable services is set at unity. In this subsection, we envisage the robustness of the result when the elasticity of substitution between nondurable consumption and consumer durable services is different from unity.

If the elasticity of substitution between nondurable consumption and consumer durable services is higher (a larger  $\eta$ ), the intratemporal substitution effect between nondurable consumption and consumer durable services is stronger. Then, in response to positive capital investment shocks, it is easier to obtain the comovement. By contrast, when the elasticity of substitution between nondurable consumption and consumer durable services is lower, the intratemporal substitution effect is weaker. Then, it is more difficult to generate comovement.

The impulse responses are displayed in Figure 5. We find that when the elasticity of substitution between nondurable consumption and consumer durable services is increased to 1.1 and larger values, nondurable consumption increases and comoves with other real variables. Moreover, when the elasticity of substitution is decreased to 0.9, nondurable consumption also comoves with investment. Yet, when the elasticity of substitution is too small, that is, smaller than 0.9, nondurable consumption decreases on impact and thus does not comove with other real variables.

#### [Insert Figure 5 here]

In general, the estimated elasticity of substitution between nondurable consumption and

<sup>&</sup>lt;sup>17</sup> Consumption prices increase as a result of a rise in the real marginal cost in the consumption sector.

consumer durable services is greater than 0.95. Using quarterly data in the US from the National Income and Product Account (NIPA) and Gordon (1990), Ogaki and Reinhart (1998a) estimated the values for  $\eta$  and obtained the range of 0.97 to 1.17 over the period 1947-1983. Moreover, Ogaki and Reinhart (1998b) estimated and obtained the value of 0.98 for  $\eta$  when they used annual data in the US from the NIPA over the period 1929-1990. Thus, to generate the comovement, the required elasticity of substitution between nondurable consumption and consumer durable services is within the range of the estimated values in the US.

#### 5.4 Elasticity of labor supply

Finally, in our baseline, the elasticity of the Frisch labor supply is set equal to unity. Our results of comovement are robust for a wide range of the elasticity of the Frisch labor supply.

If the elasticity of the Frisch labor supply is higher (a smaller  $\phi$ ), we would anticipate that hours of work are more volatile. Thus, in response to positive investment shocks, hours of work are raised by more so that output in both sectors is increased by more. By contrast, if the elasticity of the Frisch labor supply is lower, hours of work are raised by less so that output in both sectors is increased by less.

Figure 6 illustrates the impulse responses when the Frisch labor supply elasticity deviates from unity. It is clear that in response to a positive capital investment shock, output, nondurable consumption, investment and hours of work all increase by more when the Frisch labor supply elasticity is larger, and increase by less when the Frisch labor supply elasticity is smaller. We find that nondurable consumption increases and comoves with other real variables under a wide range of the elasticity of the Frisch labor supply at  $\phi \in [0, 10]$ .

#### [Insert Figure 6 here]

#### 6. Concluding remarks

Recent research based on sticky-price models suggests that capital investment shocks are an important driver of business cycle fluctuations in the postwar US economy. Despite their quantitative importance in explaining business cycle fluctuations, a comovement problem emerges because a positive capital investment shock generates an intertemporal substitution effect away from consumption and toward investment. Thus, investment increases but consumption decreases. In this paper, we estimate a VAR model and offer empirical evidence showing that consumption and investment comove in response to a positive capital investment shock. Then, we resolve the comovement problem by extending the standard neoclassical sticky-price model to a two-sector model

with consumer durable services. With consumer durable services in a two-sector sticky-price model, a positive capital investment shock also generates an intratemporal substitution effect away from consumer durable services toward nondurable consumption whose effect dominates the intertemporal substitution effect. As a result, nondurable consumption increases and comoves with investment, output, hours worked and the real wage.

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#### Appendix A.

The Appendix explains how we obtain the coefficient of the cost of price adjustment  $\vartheta_j$ . Let a variable with a cap "~" denote a percentage deviation of the variable from its steady-state level. Log-linearization of the optimal pricing condition in (6c) gives the following New Keynesian Phillips curve,

$$\tilde{\pi}_{jt} = \frac{\varepsilon_j - 1}{\vartheta_j} \tilde{\lambda}_{jt} + \beta E_t(\tilde{\pi}_{jt+1}), \quad j = C, \quad I.$$
(A.1)

where the slope is  $(\varepsilon_j - 1)/\vartheta_j$ . The slope of the New Keynesian Phillips curve in the Calvo-Yun model is  $(1-\theta_j)(1-\beta\theta_j)/\theta_j$ , where  $\theta_j$  is the probability of not resetting prices (see, for example, Equation (3) in Galí and Gertler, 1999.) By equating these two slopes, we can obtain the coefficient of the cost of price adjustment  $\vartheta_j$ .

Table 1: Parameter Set	tting	(frequency: quarterly)	
Description	Parameter	Model with consumer durables	Model without consumer durables
TFP in the consumption and investment sectors	$A_C, A_I$	1	1
Elasticity of sub. between nondurables and durables	η	1	1
Elasticity of sub. between intermediates	$\mathcal{E}_C, \mathcal{E}_I$	6	6
Share of durable services	$\mu$	0.2	0
Inverse elasticity of labor supply	$\phi$	1	1
Hours of work	L	1/3	1/3
Discount factor	β	0.99	0.99
Autocorrelation of the capital investment shock	ρ	0.72	0.72
Standard deviation of error to the investment shock	σ	0.0603	0.0603
Coefficient of inflation rates in Taylor rule	χ	1.5	1.5
Capital share in the investment sector	$\alpha_I$	0.27	0.27
Capital share in the consumption sector	$\alpha_C$	0.47	0.47
Depreciation rate of capital	$\delta_K$	0.025	0.025
Depreciation rate of consumer durable services	$\delta_D$	0.025	
Coefficient of adjustment costs in capital investment	$\varphi_K$	0.005	0.005
Coefficient of adjustment costs in consumer durable investment	$\varphi_D$	0	_
Parameter of labor in utility	ν	5.573	5.794
Coefficient of price adjustment in investment sector	$\vartheta_I$	0	0
Coefficient of price adjustment in consumption sector	$oldsymbol{artheta}_C$	96.154	96.154



Figure 1. Empirical impulse responses to a positive investment shock

Note: The horizontal axis is quarters; the vertical axis is percentage. The dashed lines indicate approximate 95-percent confidence bands.



Figure 2. Impulse responses to a positive investment shock







Figure 4. Impulse responses to a positive investment shock in the model with less sticky nondurable prices



Figure 5. Impulse responses to a positive investment shock in the models with different elasticities of substitution between consumption and consumer durable services



Figure 6. Impulse responses to a positive investment shock in the model with different elasticities of the Frisch labor supply

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